

1. You are watering the lawn and aiming the hose upward at an angle of inclination  $\theta$ . Let  $r$  be the range of the hose, that is, the distance from the hose to the point of impact of the water. Then  $r$  is given by

$$r = \frac{2v^2}{g} \sin \theta \cos \theta,$$

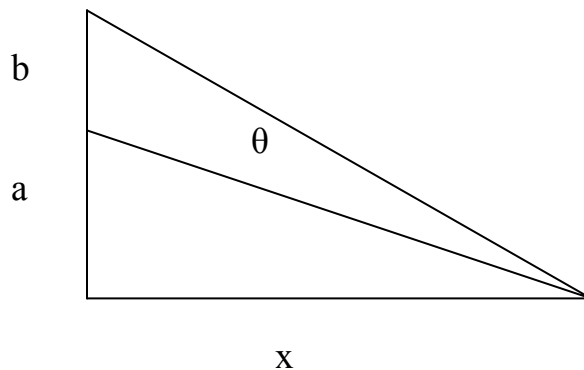
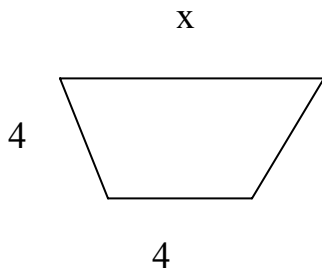
where  $v$ ,  $g$  are constants. For what angle is the range a maximum?

2. Let  $a_1, a_2, \dots, a_n$  be numbers. Show that there is a single number  $x$  such that

$$(x - a_1)^2 + (x - a_2)^2 + \dots + (x - a_n)^2$$

is a minimum and find this number.

3. A piece of wire of length  $L$  is cut into two parts, one of which is bent into the shape of an equilateral triangle and the other into the shape of a circle. How should the wire be cut so that the sum of the enclosed areas is:
- a minimum?
  - a maximum?
4. A 400 meter track is to be constructed with two parallel straightaways of length  $s$  joining two semi-circular curves of radius  $r$ . What are the dimensions of the track that will enclose the largest area?
5. If we cut four congruent squares out of the corners of a square piece of cardboard 12 inches on each side, we can fold up the four remaining flaps to obtain a tray without a top. What size squares should be cut out in order to maximize the volume of the tray?
6. An irrigation channel made of concrete is to have a cross section in the form of an isosceles trapezoid, three of whose sides are 4 feet long. How should the trapezoid be shaped if it is to have the maximum possible area? (Consider the area as a function of  $x$  and solve.)
7. The base of a painting on a wall is  $a$  feet above the eye of an observer. The vertical side of the painting is  $b$  feet long. How far from the wall should the observer stand to maximize the angle that the painting subtends?



Name \_\_\_\_\_

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**Mike Huff**  
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